

# Image Processing

Summary

# Themes

1. Human Seeing
2. Filtering
3. Morphological Operations
4. Fourier Transform
5. Diffusion Filters
6. Continuous Energy Minimization
7. Discrete Energy Minimization
8. Interest Points
9. Image Features
10. 3D-Geometry
11. RANSAC
12. Stereo
13. Tracking

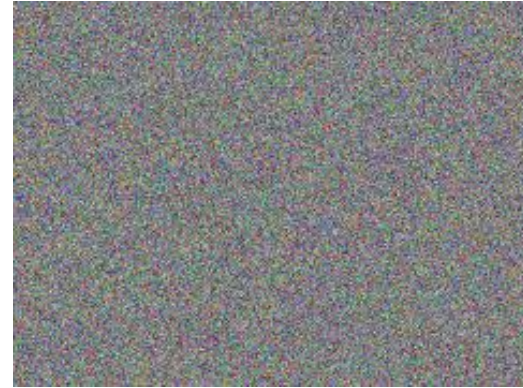


# Filtering

## Image generation



Original

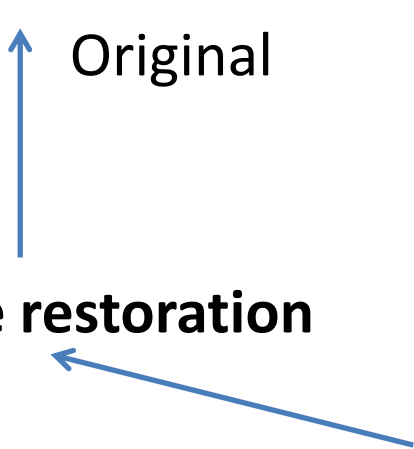


Noise



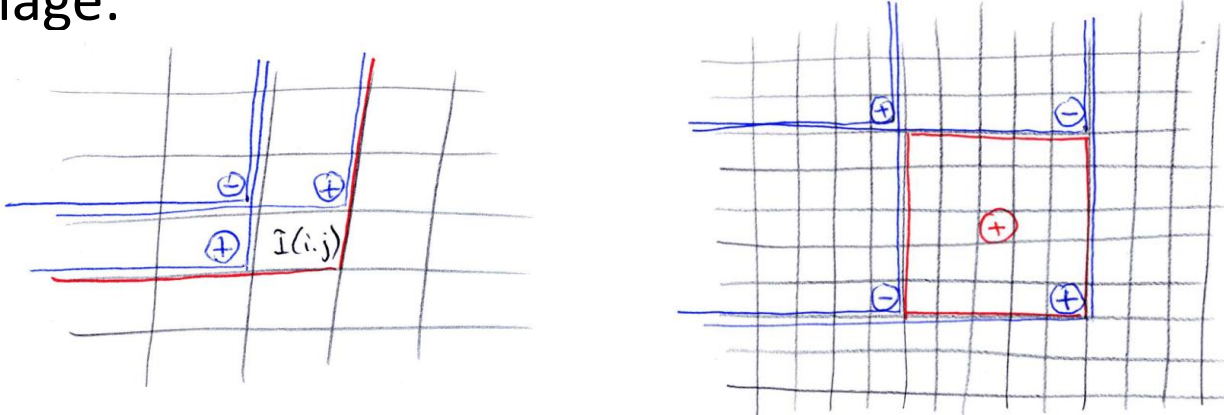
Result

## Image restoration



# Filtering

Integral Image:



Useful (efficient) for Mean-Filtering, Harris Detector, Haar Features and many more ...

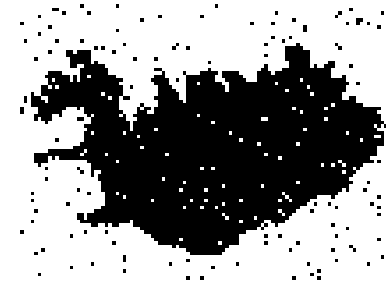
Convolution techniques, separable filters, box-filter, ...

Use filtering with care and respect. Do not use filters without to know, what are they really doing, have in mind always the whole:

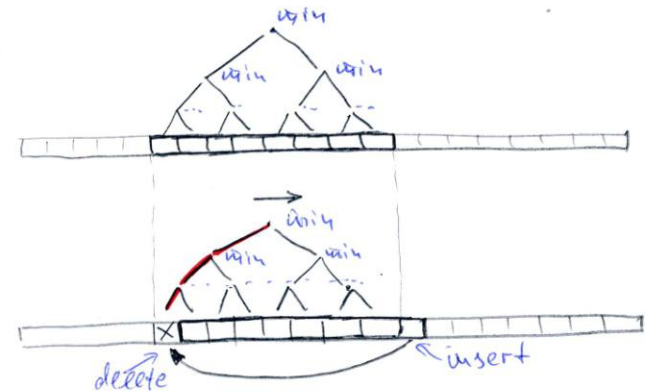
Model  $\rightarrow$  Formal task  $\rightarrow$  Solution  $\rightarrow$  Algorithm (program)

# Morphological Operations

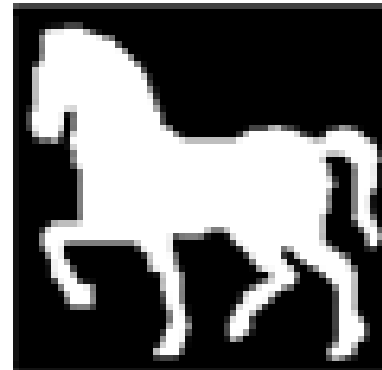
Dilation, erosion, opening, closing  
structuring elements



Fast algorithms



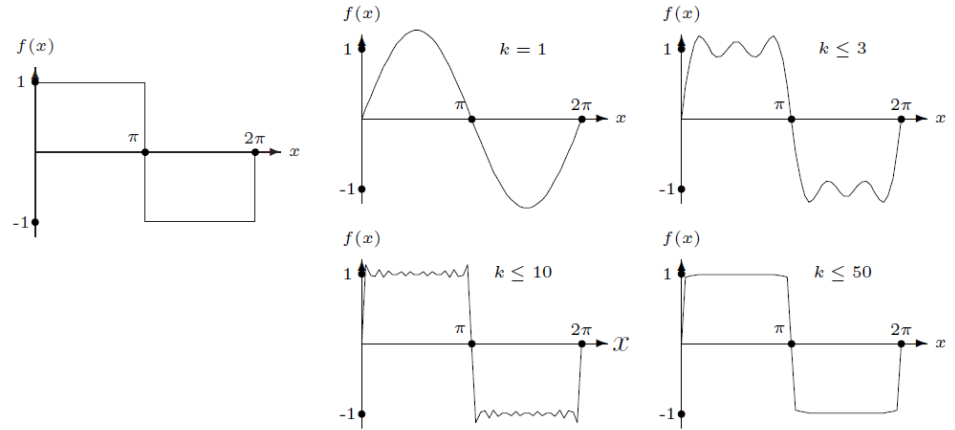
Distance transform  
structuring functions



# Fourier Transform

## Bases in function spaces – Math

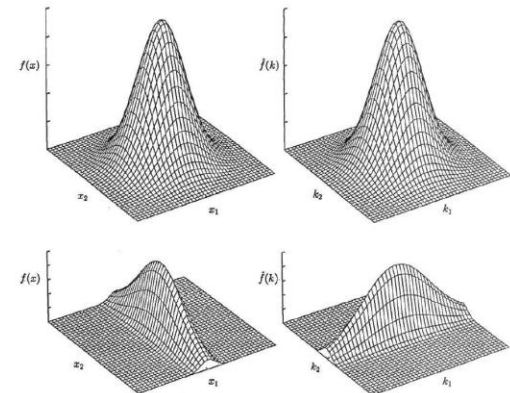
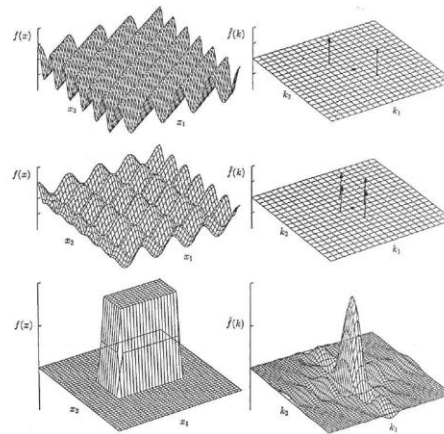
## Fourier transform



## Convolution theorem + consequences

$$\mathcal{F}[f * g] = \mathcal{F}[f] \cdot \mathcal{F}[g]$$

## Spectrums



# Diffusion Filters

Physical background – Fick's law, flux, tensors, gradients, divergences etc.

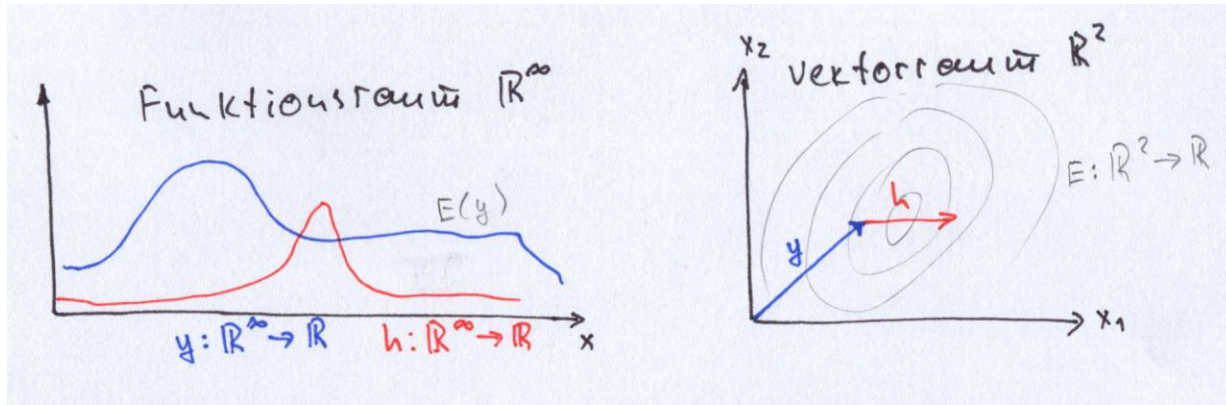
Linear, non-linear, isotropic, anisotropic diffusions, edge information for tensors, diffusivity (robust functions), TV-flow

Numerical schemes: explicit, implicit, reduction to linear systems





# Continuous Energy Minimization



Relations: continuous  $\leftrightarrow$  discrete (domain of definition, range)

Example: denoising, energy terms

Discrete domain of definition: reduction to large linear systems

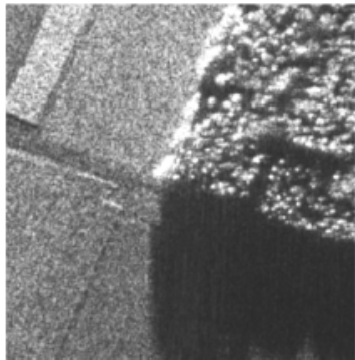
Continuous domain of definition: calculus of variations,  
Gâteaux-derivative, Euler-Lagrange equations

Relation to diffusion, regularizers



# Discrete Energy Minimization

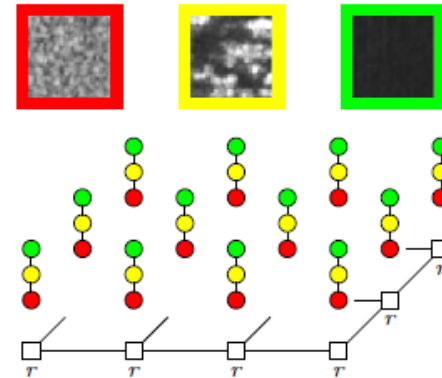
## Example: segmentation



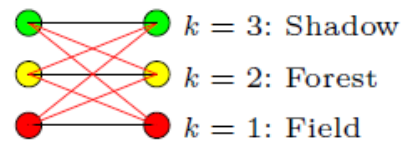
Original



A possible segmentation

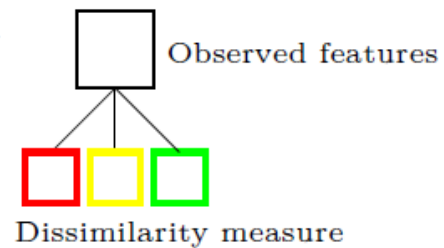


Compactness terms



— Penalty  
— Zero

Data terms

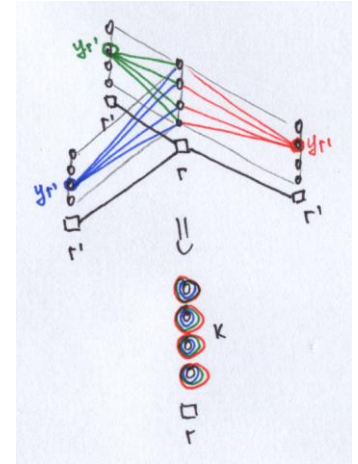


$$y^* = \arg \min_y \left[ \sum_r q_r(y_r) + \sum_{rr'} g_{rr'}(y_r, y_{r'}) \right]$$

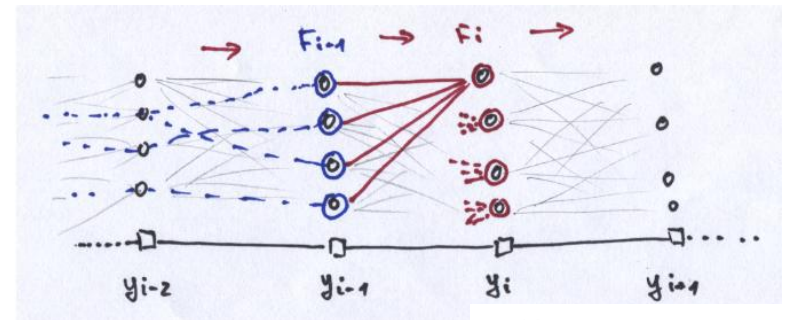
# Discrete Energy Minimization

Iterated Conditional Modes:

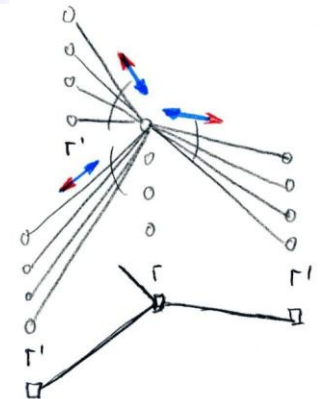
$$y_r = \arg \min_k \left[ q_r(k) + \sum_{r': rr' \in E} g_{rr'}(k, y_{r'}) \right]$$



Dynamic Programming:

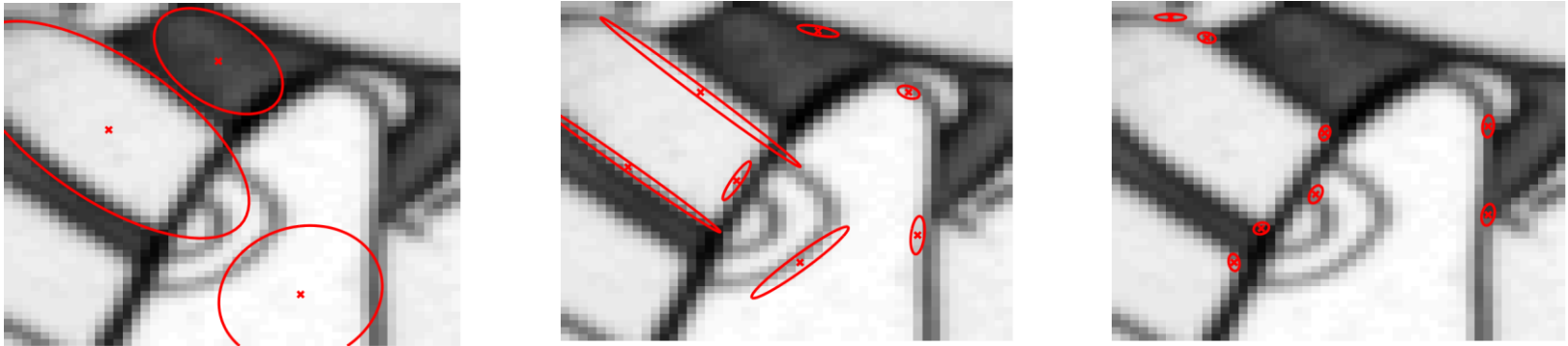


Equivalent transformations, Seeming Quality,  
Diffusion Algorithm:

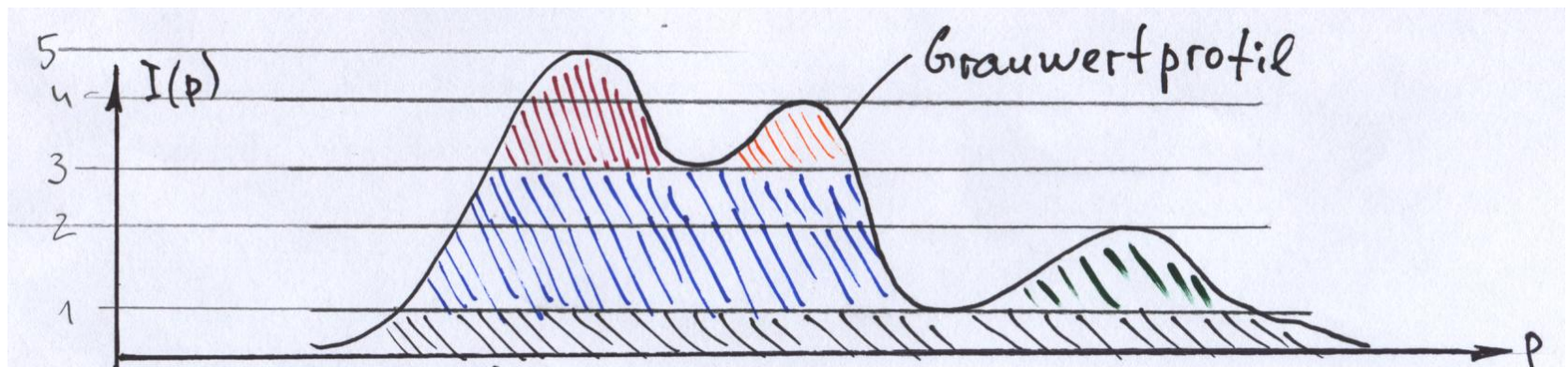


# Interest Points

Harris detector: auto-correlation function, fast algorithm

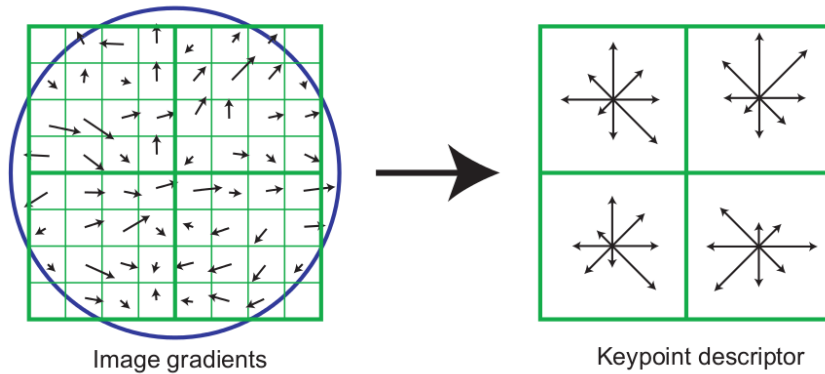


Maximally stable extremal regions (MSER): definition, properties

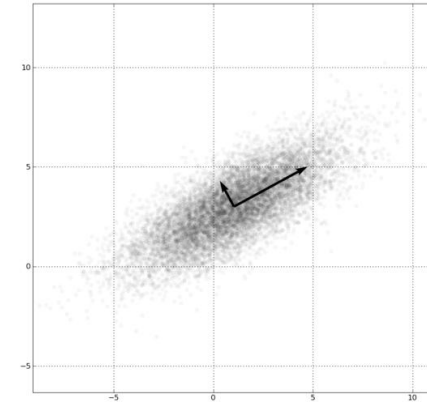


# Image Features

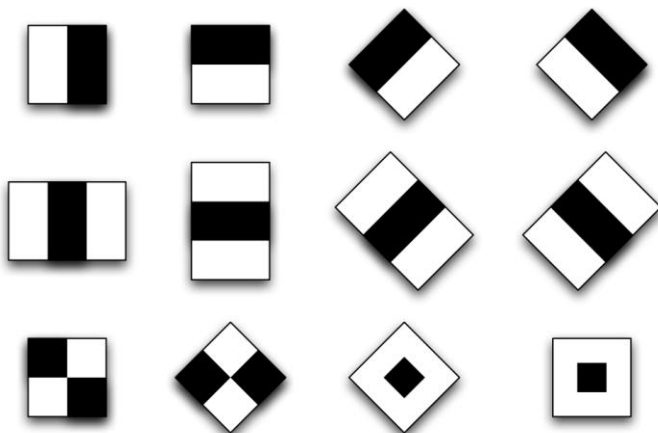
SIFT:



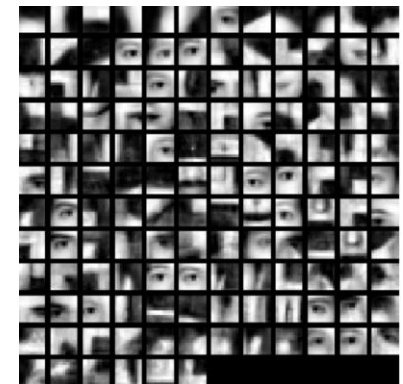
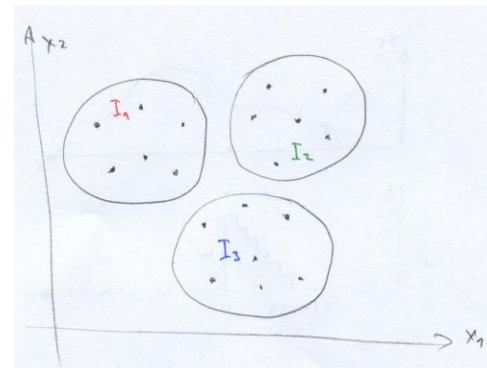
PCA:



Haar Features:

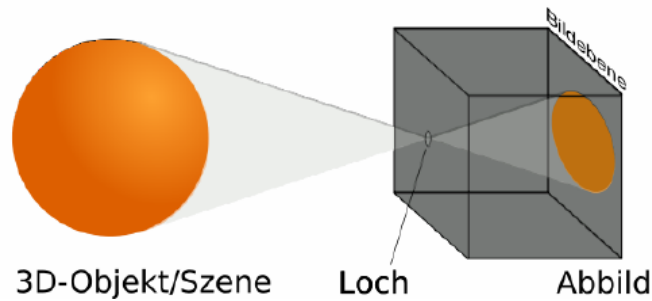


Clustering, Visual Words:

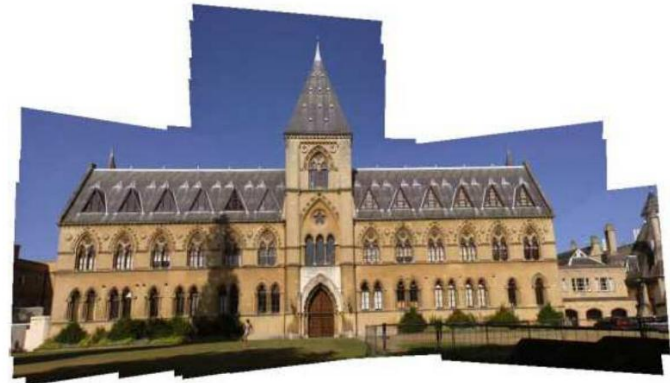
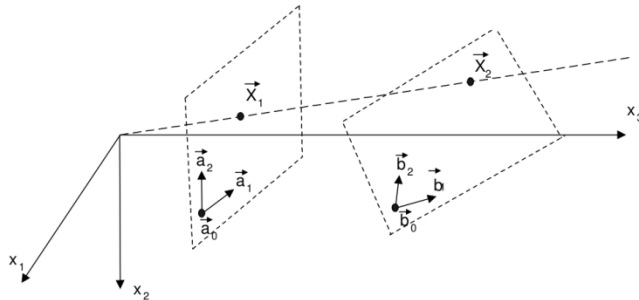


# 3D-Geometry

Pinhole camera model:

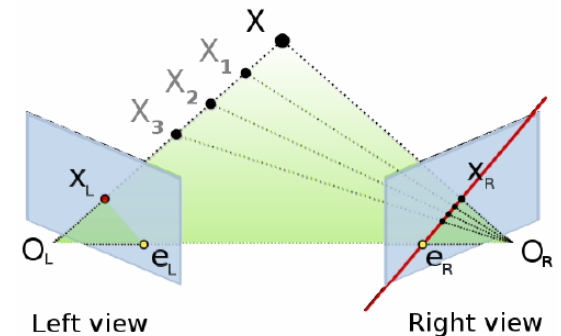


Homography:



Epipolar Geometry:

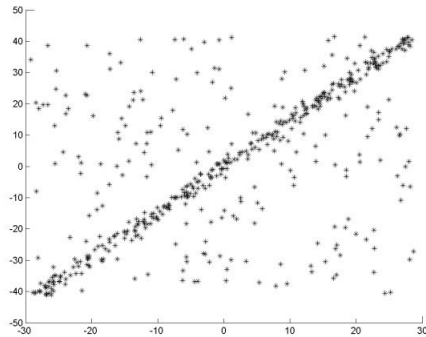
$$x_l^T F x_r = \begin{bmatrix} x_{l1} & x_{l2} & 1 \end{bmatrix} \begin{bmatrix} f_{11} & f_{12} & f_{13} \\ f_{21} & f_{22} & f_{23} \\ f_{31} & f_{32} & f_{33} \end{bmatrix} \begin{bmatrix} x_{r1} \\ x_{r2} \\ 1 \end{bmatrix} = 0$$





# RANSAC

## Model fitting, Outliers:



## Algorithm:

Wiederhole oft

Würfele  $L' \subset L$ ,  $|L'| = d$

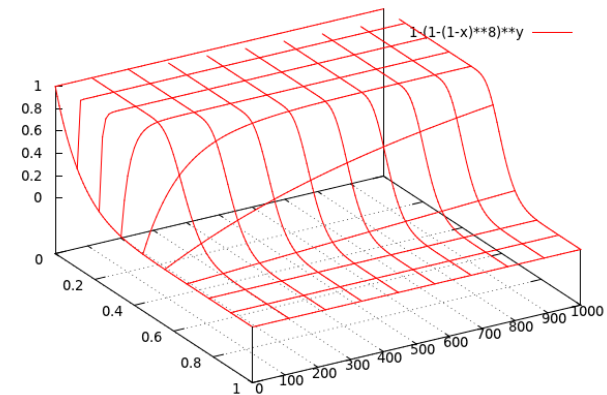
Schätze  $y = g(L')$

Bewerte  $f(y) = \sum_i f(x^i, y)$

wenn  $f(y) > f(y^*)$

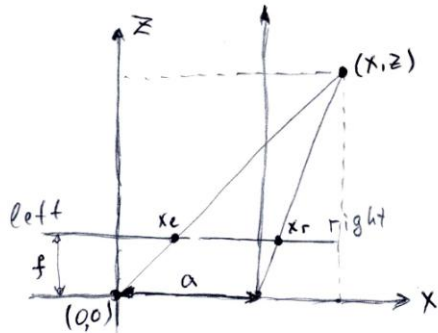
setze  $y^* = y$  und merke  $f(y^*)$

## Convergence:



# Stereo

Disparities:



$$\frac{Z}{f} = \frac{X}{x_e} ; \quad \frac{Z}{f+a} = \frac{X-a}{x_r}$$

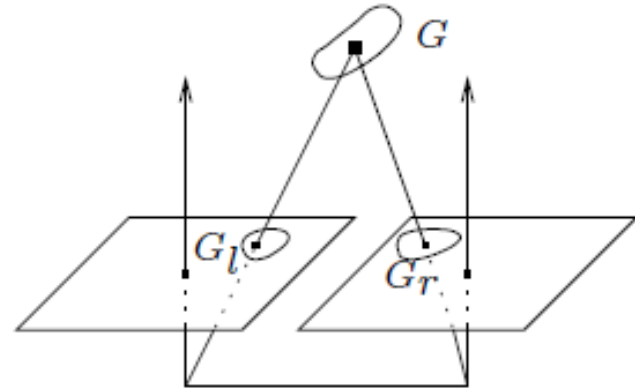
$$\frac{X}{x_e} = \frac{X-a}{x_r}$$

$$X = \frac{a \cdot x_e}{x_e - x_r}$$

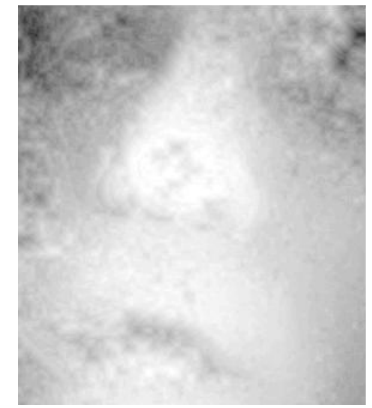
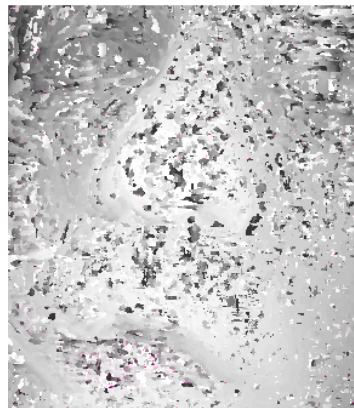
$$Z = \frac{f \cdot X}{x_e} = \frac{f \cdot a}{x_e - x_r}$$

disparity

Dissimilarity measures:



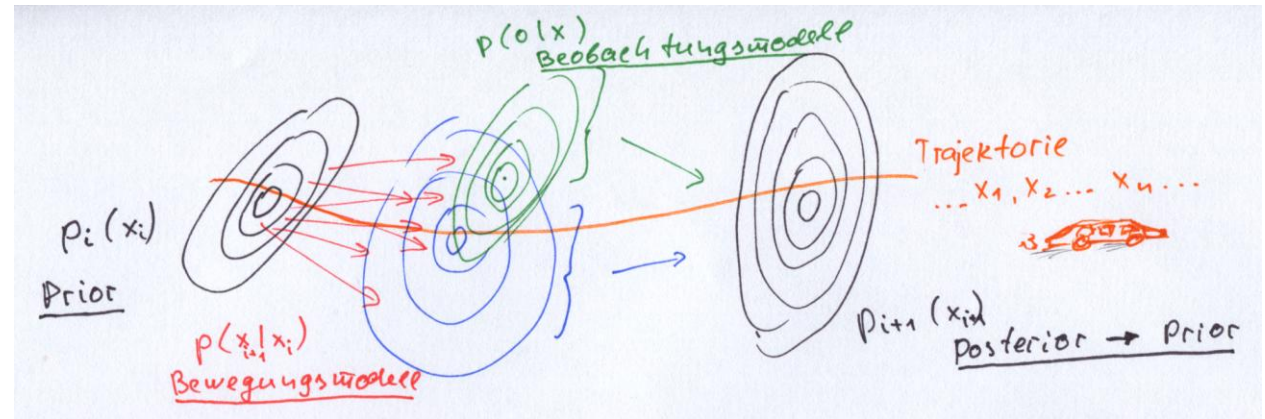
Block Matching  $\rightarrow$  Row-wise stereo  $\rightarrow$  Energy Minimization





# Tracking

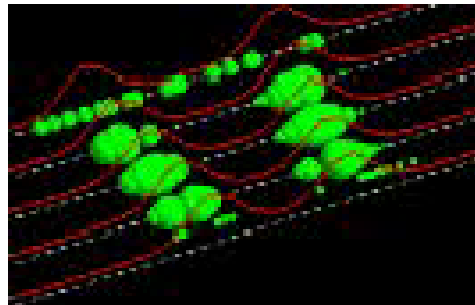
## Bayesian Filtering:



## Kalman Filter:

$$\begin{bmatrix} x_{i+1} \\ y_{i+1} \\ v_{x,i+1} \\ v_{y,i+1} \end{bmatrix} = \begin{bmatrix} 1 & 0 & \Delta t & 0 \\ 0 & 1 & 0 & \Delta t \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x_i \\ y_i \\ v_{x,i} \\ v_{y,i} \end{bmatrix} + \epsilon \quad \begin{bmatrix} o_{x,i+1} \\ o_{y,i+1} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix} \cdot \begin{bmatrix} x_i \\ y_i \\ v_{x,i} \\ v_{y,i} \end{bmatrix} + \delta$$

## Particle Filtering:



New Prof. – Carsten Rother

New courses:

**Computer Vision** (Carsten Rother):



similar to Image Processing, but with “more CV”: more geometry (especially 3D), image formation and cameras, motion estimation (Optical Flow), recognition, Pictorial Structures ...

Practice: different compared to IP – more structured:  
There are three block, each one consisting of a “lecture” (fast implementations, algorithmic tricks and techniques etc.) and “free work” (assignment).

Combination BV(SS2013)+CV(W2013/2014) is allowed for exams.

## **Machine Learning** (Dmitrij Schlesinger):

Almost the same as Pattern Recognition, but:

- a bit less Neural Networks,
- more Machine Learning: regressions, other learning principles (e.g. reinforcement learning), other classifiers (e.g. decision trees) etc.

Combination ME(SS2013)+ML(W2013/2014) is not allowed.

Other courses (Holger Heidrich with others):

- Einführungspraktikum Computer Vision
- Komplexpraktikum Computer Vision
- Projektpraktikum Computer Vision
- Hauptseminar Bildanalyse