

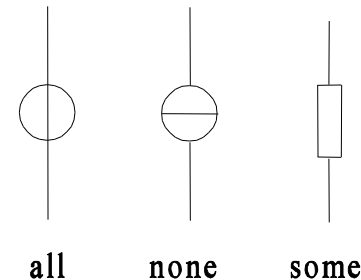
3. Solution of a resistive network

Tree:

A **tree** is a set of network branches including all nodes without forming a loop. (A **cotree** is the complementary set to a tree which does not form a cutset.)

Choose a **tree**, which contains

- **all** voltage sources,
- **no** current source,
- **some** resistors.



If possible choose resistors such that

- **all** tree resistors are **current controlled**, $v=r(i)$, while
- **all cotree** resistors are **voltage controlled**, $i=g(v)$.

3. Solution of a resistive network

Every cotree branch closes a **loop**.

This leads to the set of $b-n+1$ linearly independent loop equations.

$$(\mathbf{v}_{co}, \mathbf{v}_{is}) = L_{loop}(\mathbf{v}_{tr}, \mathbf{e}_{tr}(t)) \quad (\mathbf{e}_{tr}(t) - \text{voltage sources of the tree})$$

Every tree branch forms a **cutset**.

This leads to the set of $n-1$ linearly independent cutset equations.

$$(\mathbf{i}_{tr}, \mathbf{i}_{vs}) = L_{cut}(\mathbf{i}_{co}, \mathbf{e}_{co}(t)) \quad (\mathbf{e}_{co}(t) - \text{current sources of the cotree})$$

Now the resistor equations, $i=g(v)$ or $v=r(i)$, lead to a **reduced equation system**:

NR instead of $2b$ variables, namely \mathbf{v}_{tr} (voltages of the tree resistors) and \mathbf{i}_{co} (currents of the cotree resistors).

If the tree (cotree) resistors are current (voltage) controlled \rightarrow explicit form:

$$\begin{aligned} \mathbf{i}_{co} &= g(\mathbf{v}_{co}) = g(\mathbf{v}_{tr}, \mathbf{e}_{tr}(t)) \\ \mathbf{v}_{tr} &= r(\mathbf{i}_{tr}) = r(\mathbf{i}_{co}, \mathbf{e}_{co}(t)) \end{aligned}$$